

Practice 4b.

Find the indicated critical z value.

- 1) Find the critical value  $z_{\alpha/2}$  that corresponds to a 98% confidence level. 1) \_\_\_\_\_  
 A) 2.05                      B) 2.33                      C) 1.75                      D) 2.575

Inverse normal (on calculator), with area =  $\alpha/2$

$\alpha = 1 - 0.98 = 0.02$  Therefore,  $\alpha/2 = 0.02/2 = 0.01$  and  $\mu = 0, \sigma = 1$  (default values for z scores)

Express the confidence interval using the indicated format.

- 2) Express the confidence interval  $0.061 < p < 0.579$  in the form of  $\hat{p} \pm E$ . 2) \_\_\_\_\_  
 A)  $0.259 \pm 0.32$               B)  $0.259 - 0.32$               C)  $0.32 \pm 0.259$               D)  $0.259 \pm 0.5$

$\hat{p} = (\text{lower bound} + \text{upper bound})/2 = (0.061 + 0.579)/2 = 0.32$

$E = (\text{Upper bound} - \text{Lower bound})/2$

$E = (0.579 - 0.061)/2 = 0.259$

Assume that a sample is used to estimate a population proportion p. Find the margin of error E that corresponds to the given statistics and confidence level. Round the margin of error to four decimal places.

- 3) 90% confidence; n = 430, x = 80 3) \_\_\_\_\_  
 A) 0.0368                      B) 0.0309                      C) 0.0331                      D) 0.0386

Calculators: 1PropZInt with n = 430, x = 80, C-Level: 0.90

Obtain the interval: 0.15517, 0.21691 and  $E = (\text{Upper bound} - \text{Lower bound})/2 = 0.0617/2 = 0.03087$

Use the given degree of confidence and sample data to construct a confidence interval for the population proportion p.

- 4) n = 96, x = 43; 98% confidence 4) \_\_\_\_\_  
 A)  $0.329 < p < 0.567$                       B)  $0.330 < p < 0.566$   
 C)  $0.348 < p < 0.548$                       D)  $0.349 < p < 0.547$

Calculators: 1PropZInt with n = 96, x = 43, C-Level: 0.98

Use the given data to find the minimum sample size required to estimate the population proportion.

- 5) Margin of error: 0.044; confidence level: 95%;  $\hat{p}$  and  $\hat{q}$  unknown 5) \_\_\_\_\_  
 A) 352                      B) 405                      C) 497                      D) 635

Sample size formula (proportions),  $n = (z_{\alpha/2})^2 * 0.25/E^2 = 1.96^2 * 0.25 / 0.044^2 = 496.07 = 497$

Notice that for sample size determination we always round the result up.

- 6) Margin of error: 0.03; confidence level: 95%; from a prior study,  $\hat{p}$  is estimated by the decimal equivalent of 66%. 6) \_\_\_\_\_  
 A) 958                      B) 2817                      C) 1654                      D) 862

Sample size formula (proportions),  $n = (z_{\alpha/2})^2 * \hat{p} * \hat{q} / E^2 = 1.96^2 * .66 * 0.34 / 0.03^2 = 957.83 = 958$

Use the given degree of confidence and sample data to construct a confidence interval for the population proportion  $p$ .

- 7) A survey of 865 voters in one state reveals that 408 favor approval of an issue before the legislature. 7) \_\_\_\_\_  
Construct the 95% confidence interval for the true proportion of all voters in the state who favor approval.  
A)  $0.444 < p < 0.500$  B)  $0.471 < p < 0.472$   
C)  $0.438 < p < 0.505$  D)  $0.435 < p < 0.508$

Calculators: 1PropZInt with  $n = 865$ ,  $x = 408$ , C-Level: 0.95

Use the given degree of confidence and sample data to construct a confidence interval for the population mean  $\mu$ . Assume that the population has a normal distribution.

- 8)  $n = 10$ ,  $\bar{x} = 12.7$ ,  $s = 3.7$ , 95% confidence 8) \_\_\_\_\_  
A)  $10.09 < \mu < 15.31$  B)  $10.05 < \mu < 15.35$   
C)  $10.07 < \mu < 15.33$  D)  $10.56 < \mu < 14.84$

T interval with:  $\bar{x} = 12.7$ ,  $s_x = 3.7$ ,  $n = 10$ , C-Level: 0.95

- 9) A laboratory tested twelve chicken eggs and found that the mean amount of cholesterol was 198 milligrams with  $s = 10.5$  milligrams. Construct a 95% confidence interval for the true mean cholesterol content of all such eggs. 9) \_\_\_\_\_  
A)  $191.4 \text{ mg} < \mu < 204.6 \text{ mg}$  B)  $191.2 \text{ mg} < \mu < 204.8 \text{ mg}$   
C)  $192.6 \text{ mg} < \mu < 203.4 \text{ mg}$  D)  $191.3 \text{ mg} < \mu < 204.7 \text{ mg}$

T interval with:  $\bar{x} = 198$ ,  $s_x = 10.5$ ,  $n = 12$ , C-Level: 0.95

- 10) The amounts (in ounces) of juice in eight randomly selected juice bottles are: 10) \_\_\_\_\_  
 $15.3 \ 15.3 \ 15.7 \ 15.7$   
 $15.3 \ 15.9 \ 15.3 \ 15.9$   
Construct a 98% confidence interval for the mean amount of juice in all such bottles.  
A)  $15.17 \text{ oz} < \mu < 15.93 \text{ oz}$  B)  $15.27 \text{ oz} < \mu < 15.83 \text{ oz}$   
C)  $15.83 \text{ oz} < \mu < 15.27 \text{ oz}$  D)  $15.93 \text{ oz} < \mu < 15.17 \text{ oz}$

T interval with raw data. Enter data on List 1, then proceed with T-Interval.

Use the confidence level and sample data to find a confidence interval for estimating the population  $\mu$ . Round your answer to the same number of decimal places as the sample mean.

- 11) Test scores:  $n = 79$ ,  $\bar{x} = 65.0$ ,  $\sigma = 5.0$ ; 98% confidence 11) \_\_\_\_\_  
A)  $64.1 < \mu < 65.9$  B)  $63.5 < \mu < 66.5$  C)  $63.7 < \mu < 66.3$  D)  $63.9 < \mu < 66.1$

Interval for means,  $\sigma$  given; therefore, this is a Z-Interval with  $n = 79$ ,  $\bar{x} = 65.0$ ,  $\sigma = 5.0$ ; C-Level: 0.98

Use the given information to find the minimum sample size required to estimate an unknown population mean  $\mu$ .

- 12) Margin of error: \$134, confidence level: 95%,  $\sigma = \$575$  12) \_\_\_\_\_  
A) 62 B) 71 C) 50 D) 100

Sample size, mean:  $n = [(z_{\alpha/2} * \sigma)/E]^2 = [(1.96 * 575)/134]^2 = 70.7 = 71$

Notice that for sample size determination we always round the result up.

## Answer Key

Testname: PRACTICE4B

- 1) B
- 2) C
- 3) B
- 4) B
- 5) C
- 6) A
- 7) C
- 8) B
- 9) D
- 10) B
- 11) C
- 12) B