

1. Given the population mean, $\mu = 32$; and, the population standard deviation, $\sigma = 2.25$, find:
 - a) Probability of $x < 30$.
 - b) Probability of $x > 35$.
 - c) Probability of x greater than 30 and less than 35; that is $P(30 < x < 35)$
 - d) If we choose 56 values of the random variable at random, and the sample mean is = 33, considering that the population standard deviation is 2.25, what is the probability that samples of the same size are less than 33?
 - e) What is the x value that is above 99% of all other values of the variable?

Press 2nd DIST:

```

0:1/2 DRAW
1:normalpdf(
2:normalcdf(
3:invNorm(
4:tpdf(
5:tcdf(
6:X2pdf(
7:X2cdf(

```

- a) Probability of $x < 30$:

You need to remember the Syntax, in the given order: Normalcdf(lower, upper, μ , σ).

Choosing normalcdf:

```

normalcdf(-E99,3
0,32,2.25)
.1870313608

```

The lower bound is negative infinite, represented by $-EE99$ (Press the little negative, then 2nd, then the comma key, and then 99). For negative infinite you may also enter -10000 or -99999.

The answer to a) is 0.1870 rounded to four decimal places.

- b) Probability of $x > 35$.

Greater than 35 means that 35 is the lower bound; the upper bound is infinity: E99. As follows:

```

normalcdf(35, E99
,32,2.25)
.0912112819

```

The answer to b) is 0.0912 rounded to four decimal places.

- c) $P(30 < x < 35)$

Lower bound is 30, upper bound is 35:

```
normalcdf(30,35,  
32,2.25)  
.7217573574
```

The answer to c) is 0.7218 rounded to four decimal places.

- d) For a random sample of the variable x , of size $n = 56$, the probability that samples of the same size are less than 33:

In this case, the Central limit theorem applies; therefore, we divide the standard deviation by the square root of the sample size. This is a question of less than a value, as follows:

```
normalcdf(-E99,3  
3,32,2.25/√(56))  
.9995593035
```

Answer: The probability that samples of size 56 are less than 33, is about 0.9996.

- e) The x value that is above 99% of all other values of the variable: In this case we know the probability or area, 0.99; choose Inverse Normal:

```
0.99 DRAW  
1:normalpdf(  
2:normalcdf(  
3:invNorm(  
4:tpdf(  
5:tcdf(  
6:χ²pdf(  
7:χ²cdf(  

```

The syntax is `invNorm(Area, μ , σ)`:

```
invNorm(0.99,32,  
2.25)  
37.23428272
```

The answer to d) is the variable x value that is above 99% of the population is $x = 37.23$, rounding to two decimal places.