

1. Find the linearization  $L(x)$  at  $x = a$ .

$$f(x) = 4x^3 - 3x + 1 \quad a = -1$$

$$L(x) = \underline{\hspace{2cm}}$$

2. Find the linearization  $L(x)$  of  $f(x) = \tan x$  at  $x = \frac{\pi}{4}$ .

The linearization is given by  $L(x) = \underline{\hspace{2cm}}$ .  
(Type an exact answer, using  $\pi$  as needed.)

3. Find the derivative of  $y$  with respect to  $x$ .

$$y = \frac{\ln(14x)}{14x}$$

$$\frac{dy}{dx} = \underline{\hspace{2cm}}$$

4. Find a linearization that will replace the function over an interval that includes the given point  $x_0$ . Center the linearization not at  $x_0$  but at a nearby integer,  $x = a$ , at which the given function and its derivative are easy to evaluate.

$$f(x) = x^3 + 4x, \quad x_0 = 0.01$$

Set the center of the linearization as  $x = \underline{\hspace{2cm}}$ .

$$L(x) = \underline{\hspace{2cm}}$$

5. Find a linearization at a suitably chosen integer near  $a$  at which the given function and its derivative are easy to evaluate.

$$f(x) = \frac{x}{x+8}, \quad a = 0.9$$

$$L(x) = \underline{\hspace{2cm}}$$

6. Find  $dy$  for  $y = 5x^6 + 9\sqrt{7x}$ .

$$dy = \underline{\hspace{2cm}}$$

7. Find  $dy$ .

$$y = \frac{3x}{1+2x^2}$$

$$dy = \underline{\hspace{2cm}} dx$$

8. Find  $dy$ .

$$y = \sin(7x^2)$$

$$dy = \underline{\hspace{2cm}} dx$$

9. Find  $dy$  for  $y = e^{\sqrt{x}+1}$ .

$$\text{For } y = e^{\sqrt{x}+1}, \quad dy = (\underline{\hspace{2cm}}) dx.$$

(Type an exact answer, using radicals as needed.)

10. Find  $dy$ .

$$y = \ln(1 + x^4)$$

$$dy = \underline{\hspace{2cm}}$$

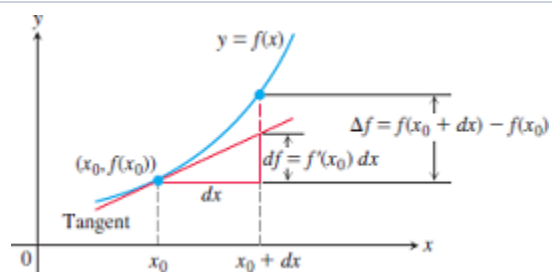
11. Find  $dy$ .

$$y = \tan^{-1}(e^{x^5})$$

$$dy = \underline{\hspace{2cm}} dx$$

12. The function  $f(x)$  changes value when  $x$  changes from  $x_0$  to  $x_0 + dx$ . Find the change  $\Delta f = f(x_0 + dx) - f(x_0)$ , the value of the estimate  $df = f'(x_0) dx$ , and the approximation error  $|\Delta f - df|$ .

$$f(x) = 7x^2 - 2x, \quad x_0 = -2, \quad dx = 0.1$$



$$\Delta f = \underline{\hspace{2cm}}$$

(Type an integer or a decimal. Do not round.)

$$df = \underline{\hspace{2cm}}$$

(Type an integer or a decimal. Do not round.)

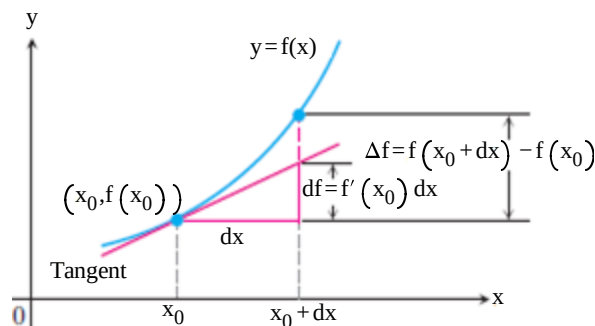
The approximation error is  $\underline{\hspace{2cm}}$ .

(Type an integer or a decimal. Do not round.)

13. The function  $f(x)$  changes value when  $x$  changes from  $x_0$  to  $x_0 + dx$ .

$$f(x) = 4x^2 + 7x - 3, \quad x_0 = 1, \quad dx = 0.1$$

- Find the change  $\Delta f = f(x_0 + dx) - f(x_0)$ .
- Find the value of the estimate  $df = f'(x_0) dx$ .
- Find the approximation error  $|\Delta f - df|$ .



a. The change  $\Delta f$  is  $\underline{\hspace{2cm}}$ .

(Type an integer or a decimal. Do not round.)

b. The value of the estimate  $df$  is  $\underline{\hspace{2cm}}$ .

(Type an integer or a decimal. Do not round.)

c. The approximation error is  $\underline{\hspace{2cm}}$ .

(Type an integer or a decimal. Do not round.)

14. The concentration  $C$  in milligrams per milliliter (mg/ml) of a certain drug in a person's blood-stream  $t$  hours after a pill is swallowed is modeled by  $C(t) = 5 + \frac{3t}{1+t^3} - e^{-0.05t}$ . Estimate the change in concentration when  $t$  changes from 30 to 50 minutes.

The change in concentration is about  $\underline{\hspace{2cm}}$  mg/ml.

(Type an integer or decimal rounded to the nearest thousandth as needed.)

1.  $9x + 9$

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2.  $1 + 2x - \frac{\pi}{2}$

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3.  $\frac{1 - \ln(14x)}{14x^2}$

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4. 0  
4x

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5.  $\frac{8}{81}x + \frac{1}{81}$

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6.  $\left( 30x^5 + \frac{63}{2\sqrt{7x}} \right) dx$

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7.  $\frac{3 - 6x^2}{(2x^2 + 1)^2}$

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8.  $14x \cos(7x^2)$

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9.  $\frac{1}{2\sqrt{x}} e^{\sqrt{x} + 1}$

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10.  $\frac{4x^3}{1 + x^4} dx$

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11.  $\frac{5x^4 e^{x^5}}{1 + e^{2x^5}}$

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12. -2.93  
-3  
0.07

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13. 1.54  
1.5  
0.04

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14. 0.609