

Find the linearization $L(x)$ of $f(x)$ at $x = a$.

1) $f(x) = 2x^2 + 4x - 1, a = 4$ 1) _____

2) $f(x) = \sqrt{6x + 4}, a = 0$ 2) _____

Find a linearization at a suitably chosen integer near a at which the given function and its derivative are easy to evaluate.

3) $f(x) = -5x^2 - 4x + 2, a = 1.1$ 3) _____

Use the linear approximation $(1 + x)^k \approx 1 + kx$, as specified.

4) Find an approximation for the function $f(x) = (1 - x)^5$ for values of x near zero. 4) _____

5) Find an approximation for the function $f(x) = \frac{3}{1 - x}$ for values of x near zero. 5) _____

6) Estimate $(1.0003)^{50}$. 6) _____

7) Estimate $\sqrt[3]{1.009}$. 7) _____

Find dy .

8) $y = 6x^2 + 9x - 3$ 8) _____

The function $f(x)$ changes value when x changes from x_0 to $x_0 + dx$. Find the approximation error $|\Delta f - df|$.

9) $f(x) = x^2, x_0 = 6, dx = 0.06$ 9) _____

Write a differential formula that estimates the given change in volume or surface area.

10) The change in the surface area $S = 4\pi r^2$ of a sphere when the radius changes from r_0 to $r_0 + dr$ 10) _____

Solve the problem.

11) A cube 5 inches on an edge is given a protective coating 0.1 inches thick. About how much coating should a production manager order for 900 cubes? 11) _____

12) $A = \pi r^2$, where r is the radius, in centimeters. By approximately how much does the area of a circle decrease when the radius is decreased from 4.0 cm to 3.8 cm? (Use 3.14 for π .) 12) _____

13) $V = \frac{4}{3}\pi r^3$, where r is the radius, in centimeters. By approximately how much does the volume of a sphere increase when the radius is increased from 1.0 cm to 1.2 cm? (Use 3.14 for π .) 13) _____

14) The diameter of a tree was 10 in. During the following year, the circumference increased 2 in. About how much did the tree's diameter increase? (Leave your answer in terms of π .) 14) _____

Answer Key

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- 1) $L(x) = 20x - 33$
- 2) $L(x) = \frac{3}{2}x + 2$
- 3) $L(x) = 7 - 14x$
- 4) $f(x) \approx 1 - 5x$
- 5) $f(x) \approx 3 + 3x$
- 6) 1.015
- 7) 1.003
- 8) $(12x + 9) dx$
- 9) 0.0036
- 10) $dS = 8\pi r_0 dr$
- 11) About 13,500 in.³
- 12) 5.0 cm²
- 13) 2.5 cm³
- 14) $\frac{2}{\pi}$ in.